

Bonds between atoms: contents

at the end of this lecture you should understand....

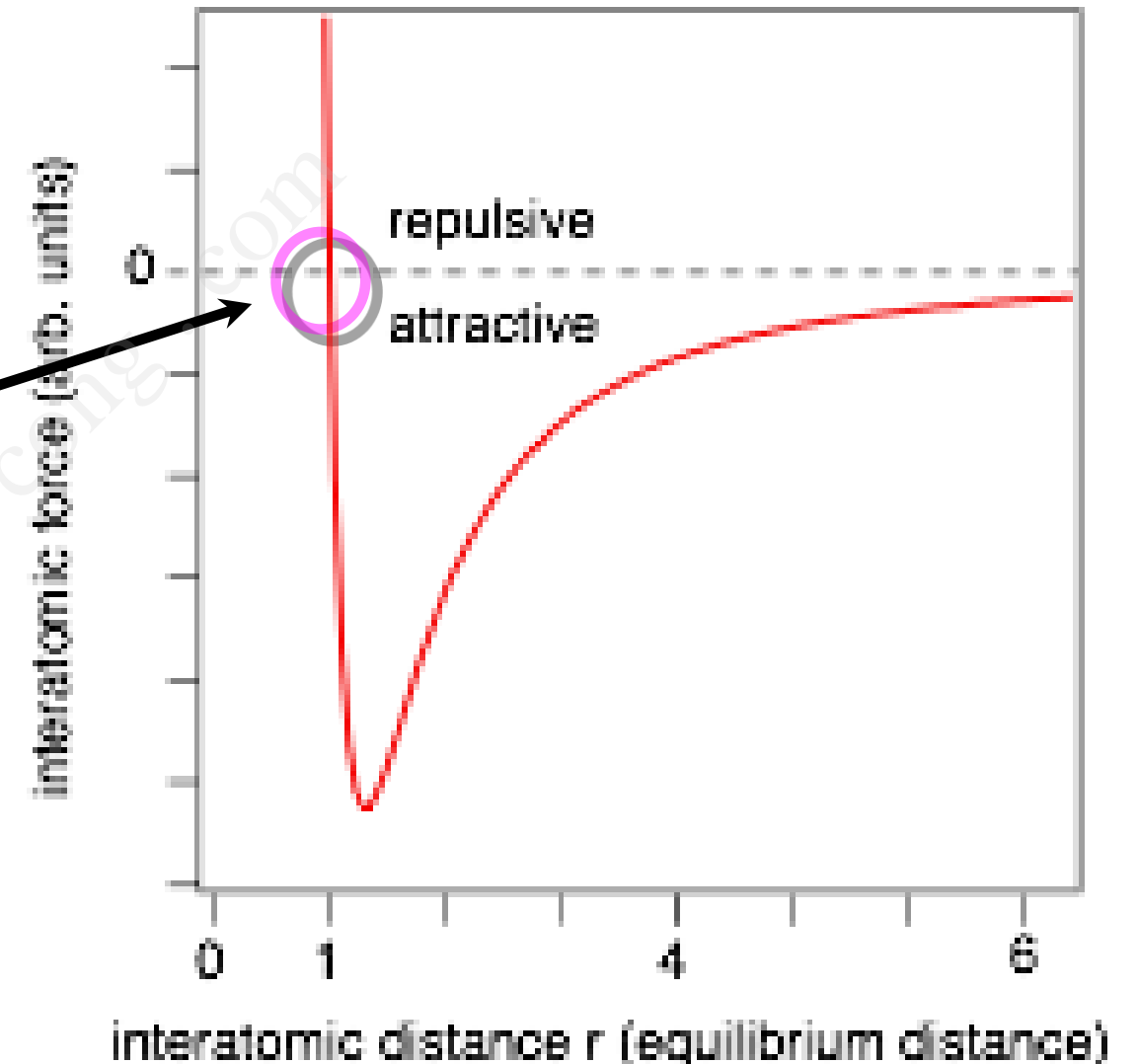
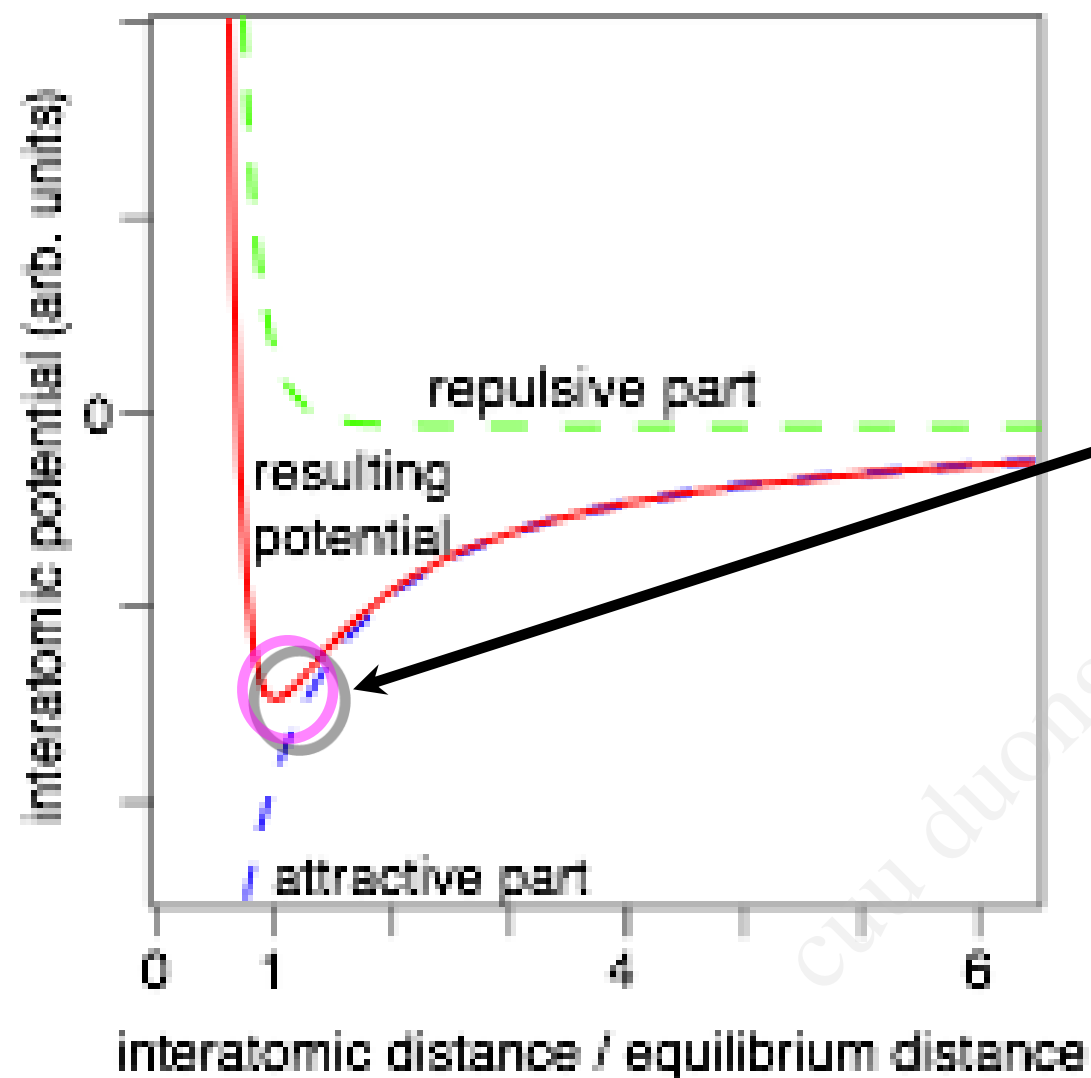
- bonding in general, attractive and repulsive forces, cohesive energy
- ionic bonding
- covalent bonding
- metallic bonding
- hydrogen bonding and van der Waals bonding
- relationship between bonding type and some physical properties of a solid (in particular melting point)

Bonding in solids: the general idea

- valence electrons (of the outer shell) achieve bonding (like in chemistry)
- decrease in total energy stabilises the solid (the solid's energy is lower than that of sum of atoms it is made of)
- so the energy gain by the bonding must be higher than the energy it costs to promote electrons from the atomic orbitals to the electronic states of the solid.
- this energy difference is a measure for the strength of the bond. It is called the **cohesive energy**.

$$\text{cohesive energy} = \text{energy of atoms} - \text{energy of solid}$$

Repulsive force



$$\phi(r) = -\frac{B}{r^m}$$

$$n > m$$

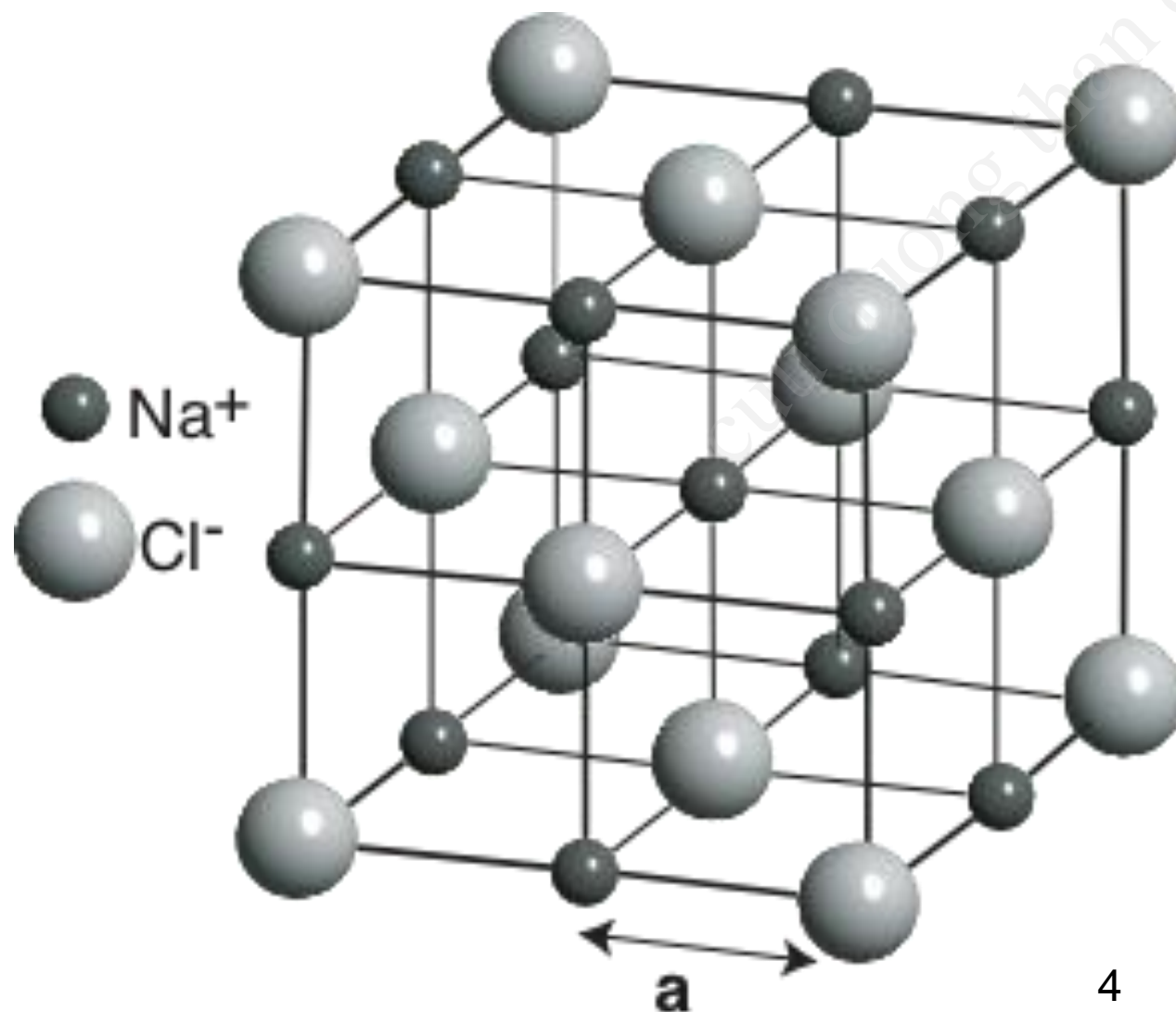
$$\mathbf{F}(\mathbf{r}) = -\text{grad}\phi(\mathbf{r})$$

$$F(r) = -\frac{d}{dr}\phi(r)$$

Ionic bonding

- form positive and negative ions (here Na^+ and Cl^-)
- bonding is achieved by electrostatic force and a classical treatment is (partially) meaningful.

example NaCl (rock salt): cubic structure



Turning Atoms in Ions

example: NaCl

how much energy does it cost?

ionization energy Na: 5.1 eV

electron affinity Cl: 3.6 eV

net energy cost: $(5.1 \text{ eV} - 3.6 \text{ eV}) = 1.5 \text{ eV}$ per pair

Ionic bonding

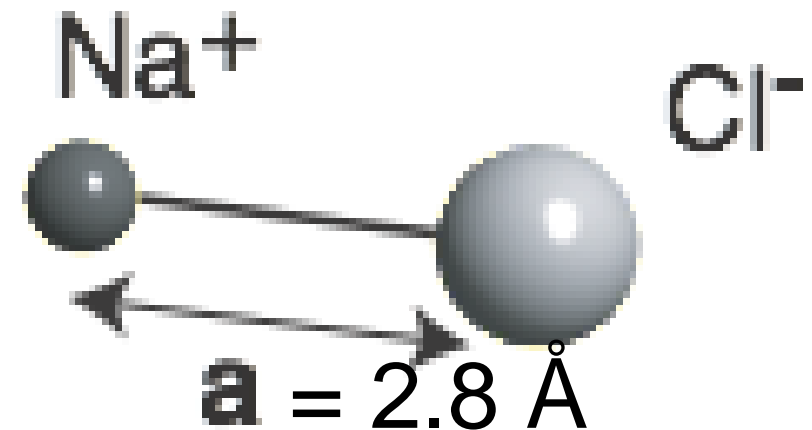
example: NaCl

what is the energy gain?

potential energy:

$$E_{Coulomb} = -\frac{e^2}{4\pi\epsilon_0 a}$$

this amounts to 5.1 eV per pair



so the total gain is
 $5.1 \text{ eV} - 1.5 \text{ eV} = 3.6 \text{ eV}$

Ionic bonding

example: NaCl

but this was just a molecule: what about the electrostatic energy gain in the solid?

consider the centre Na ion
energy gain from next 6 Cl:

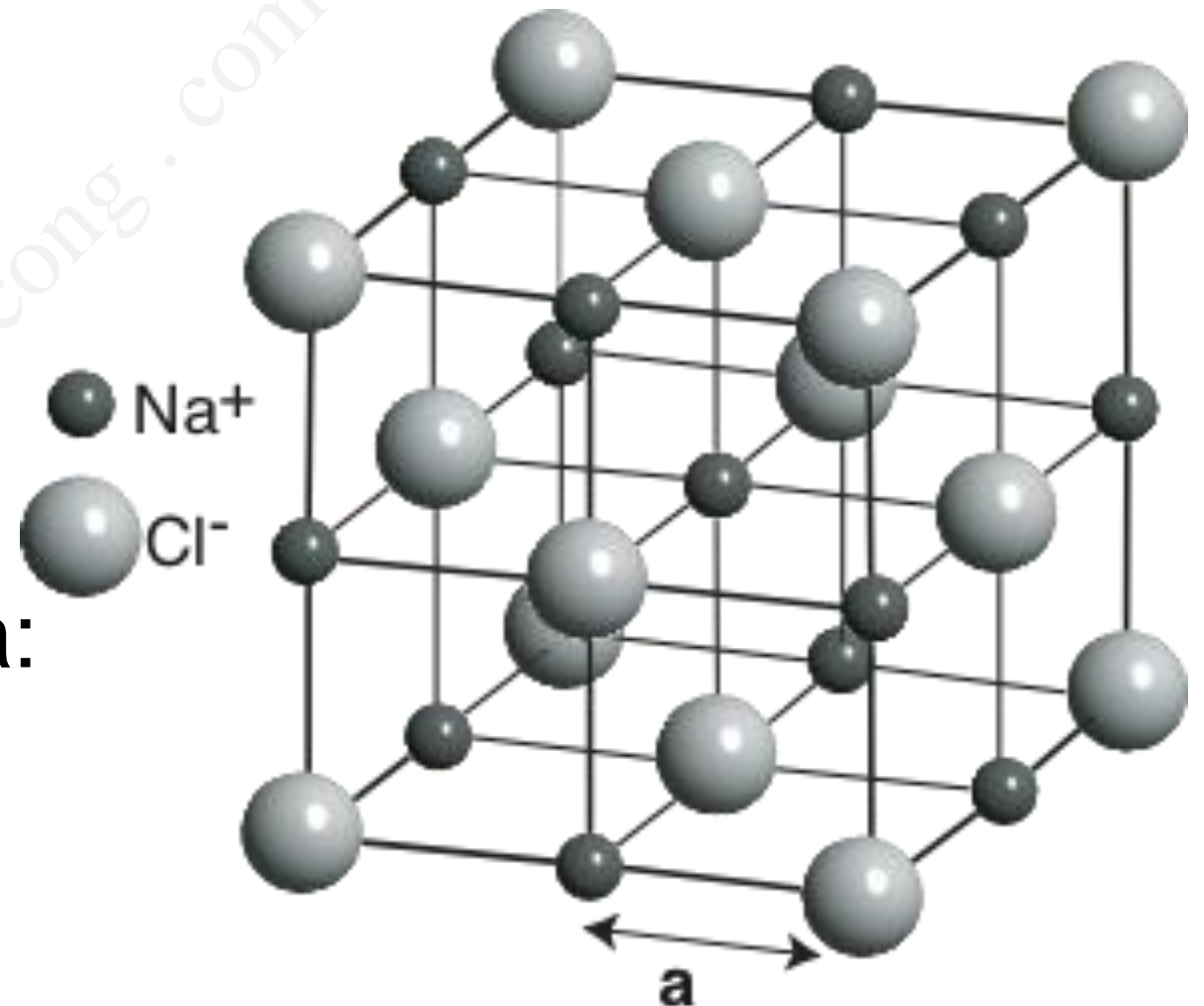
$$E = -6 \frac{e^2}{4\pi\epsilon_0 a}$$

energy loss from next 12 Na:

$$E = +12 \frac{e^2}{4\pi\epsilon_0 a \sqrt{2}}$$

next we get 8 more Cl ions and the total becomes

$$E = -\frac{e^2}{4\pi\epsilon_0 a} \times \left(6 - \frac{12}{\sqrt{2}} + \frac{8}{\sqrt{3}} \right)$$



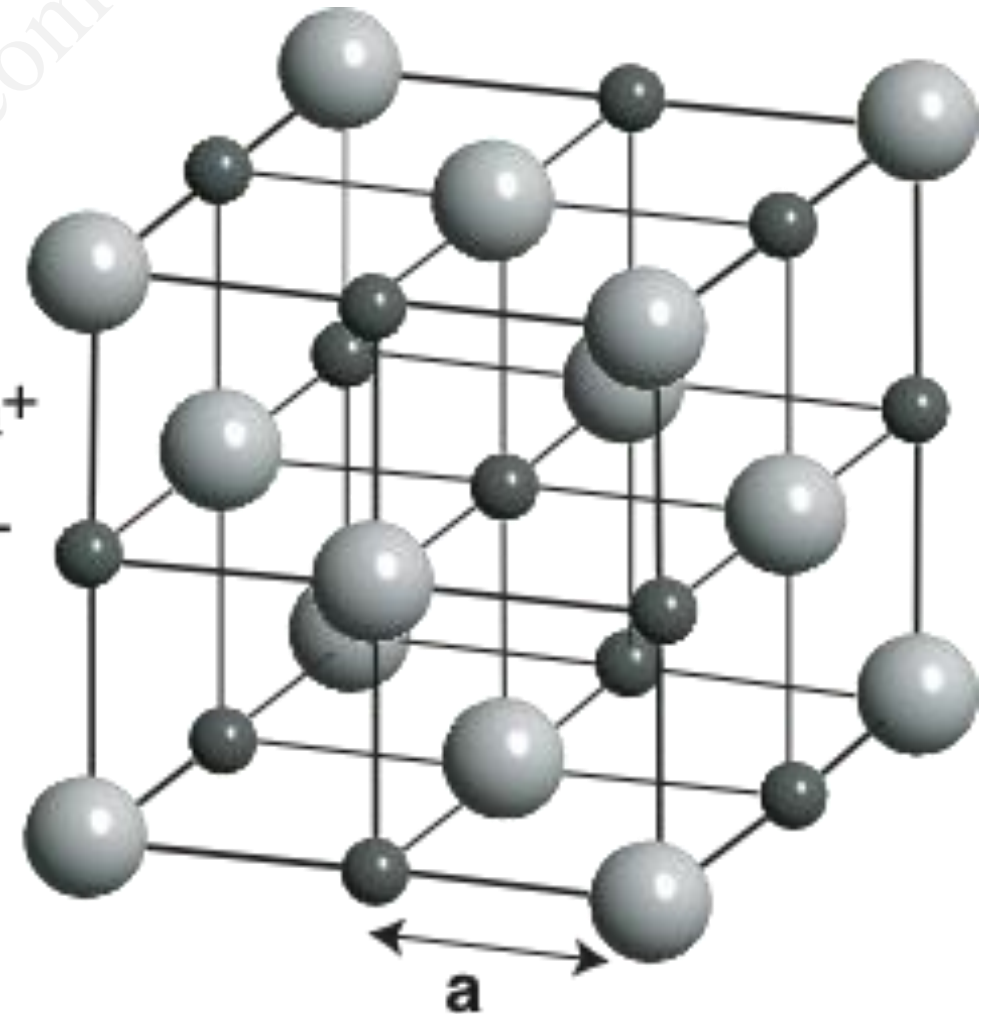
Ionic bonding

example: NaCl

eventually the series converges
and we get (for one ion)

$$E = -1.748 \frac{e^2}{4\pi\epsilon_0 a} = -M_d \frac{e^2}{4\pi\epsilon_0 a}$$

M_d is called the Madelung constant.
It is specific for a given structure.



Ionic bonding

$$E = -1.748 \frac{e^2}{4\pi\epsilon_0 a} = -M_d \frac{e^2}{4\pi\epsilon_0 a}$$

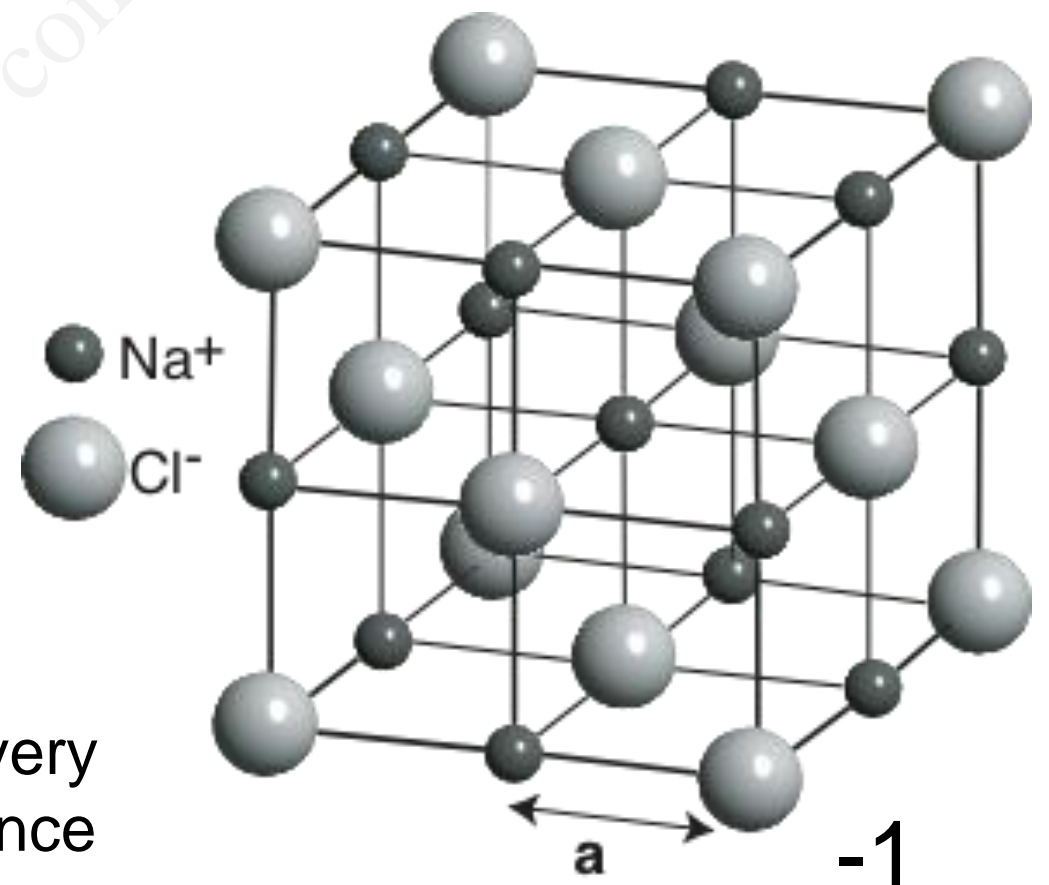
so the total lattice energy for one mole of NaCl

because there are Na and Cl ions

$$E_{tot} = \frac{2E_{Na} \times N_a}{2}$$

-1

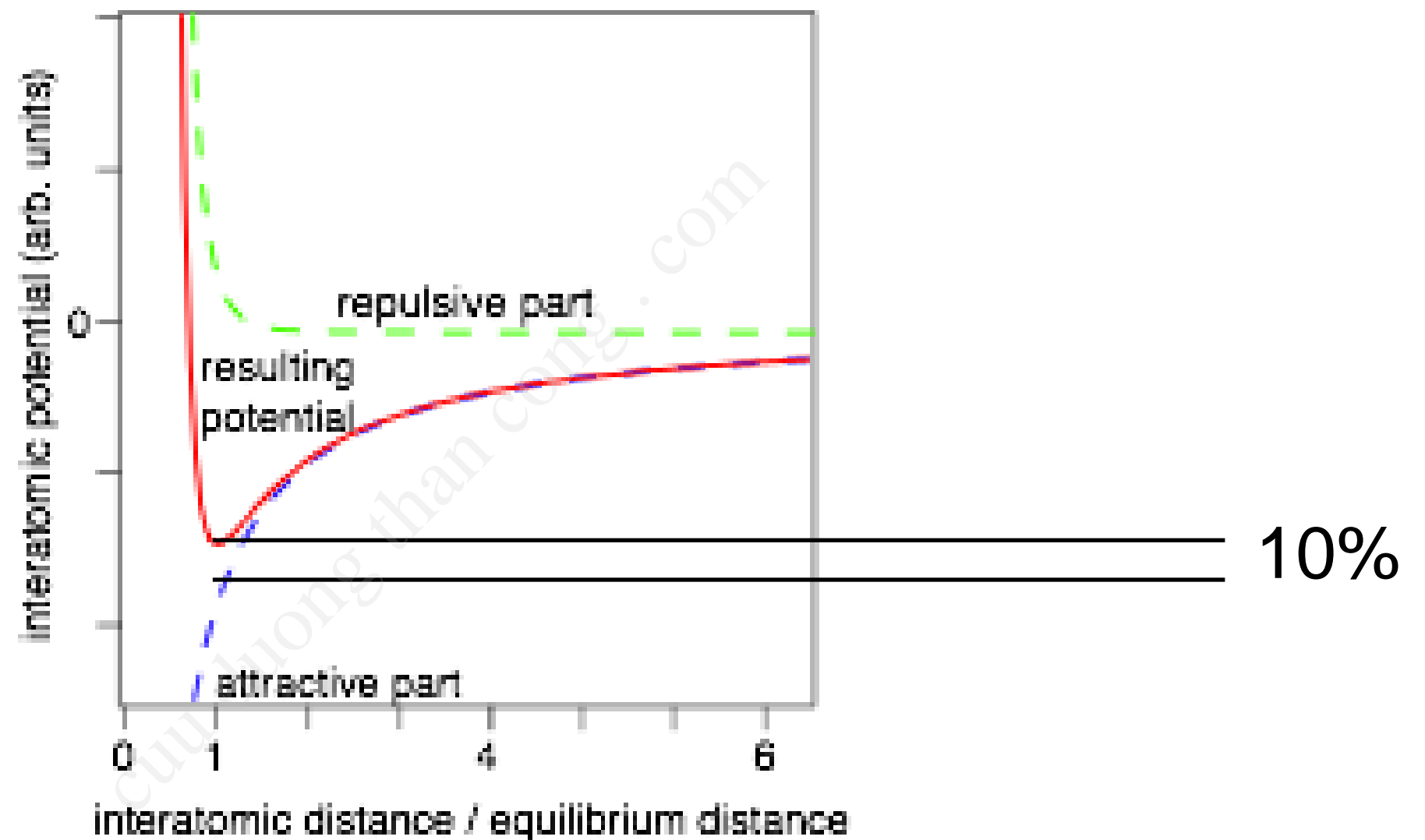
to count every pair only once



This gives 861 kJmol^{-1} . The experiment gives 776 kJmol^{-1}

Note: this is the **lattice energy**, not the **cohesive energy** (the lattice energy minus the energy to turn atoms into ions).

Repulsive force



- The existence of a (non-classical) repulsive force causes the real cohesive energy to be slightly smaller (10%) than the value calculated by the Coulomb potential.

Covalent bonding

- A detailed view on the hydrogen molecule, identical particles (later in connection with magnetism, see online note on www.philiphofmann.net).
- A simple view on other covalent bonds.

The covalent bond: simple picture

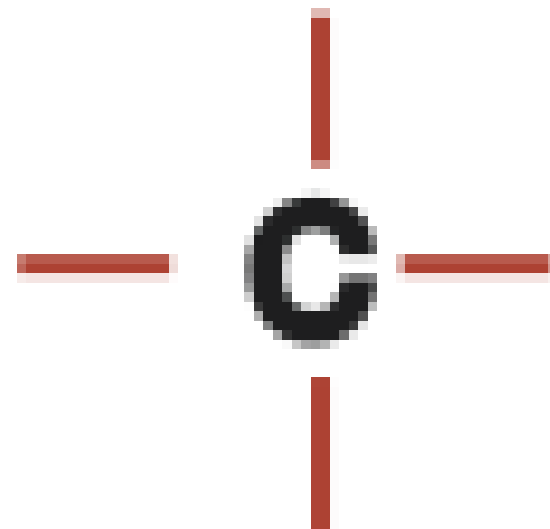
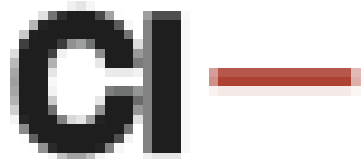


The covalent bond: less simple picture (hydrogen molecule)

$$H = -\frac{\hbar^2 \nabla_1^2}{2m} - \frac{\hbar^2 \nabla_2^2}{2m} + \frac{e^2}{4\pi\epsilon_0} \left\{ -\frac{1}{|\mathbf{R}_A - \mathbf{r}_1|} - \frac{1}{|\mathbf{R}_B - \mathbf{r}_2|} + \frac{1}{R} + \frac{1}{|\mathbf{r}_1 - \mathbf{r}_2|} - \frac{1}{|\mathbf{R}_A - \mathbf{r}_2|} - \frac{1}{|\mathbf{R}_B - \mathbf{r}_1|} \right\}$$

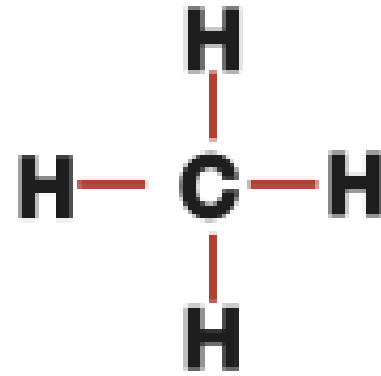
$$\Psi(\mathbf{r}_1, \mathbf{r}_2) = \frac{1}{\sqrt{2}} (\phi_A(\mathbf{r}_1)\phi_B(\mathbf{r}_2) \pm \phi_A(\mathbf{r}_2)\phi_B(\mathbf{r}_1))$$

The covalent bond: simple picture

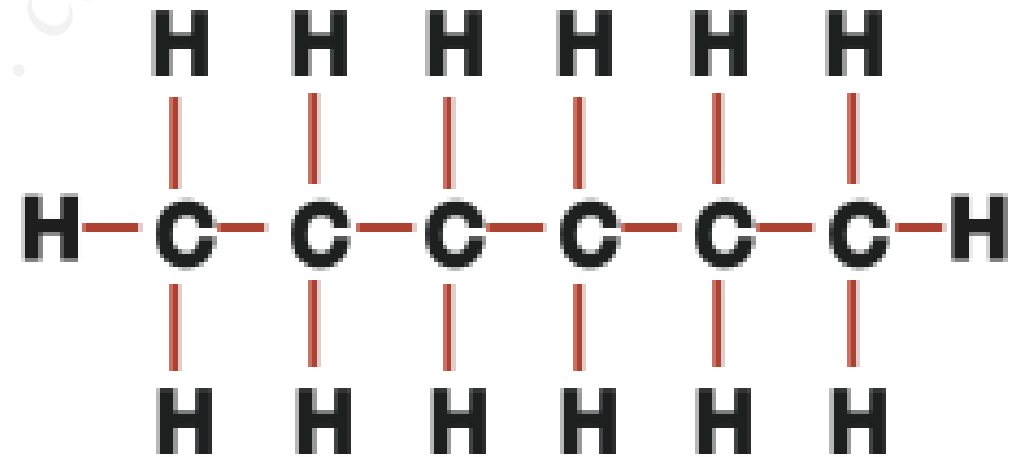
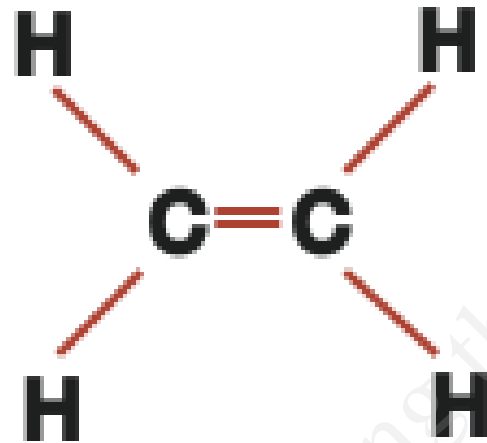


The covalent bond: simple picture

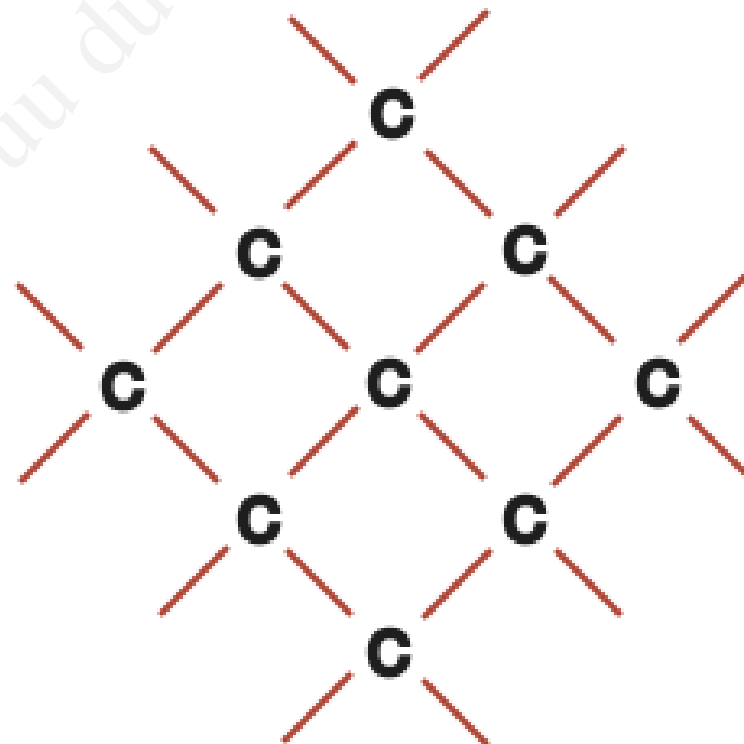
methane



hydrocarbons

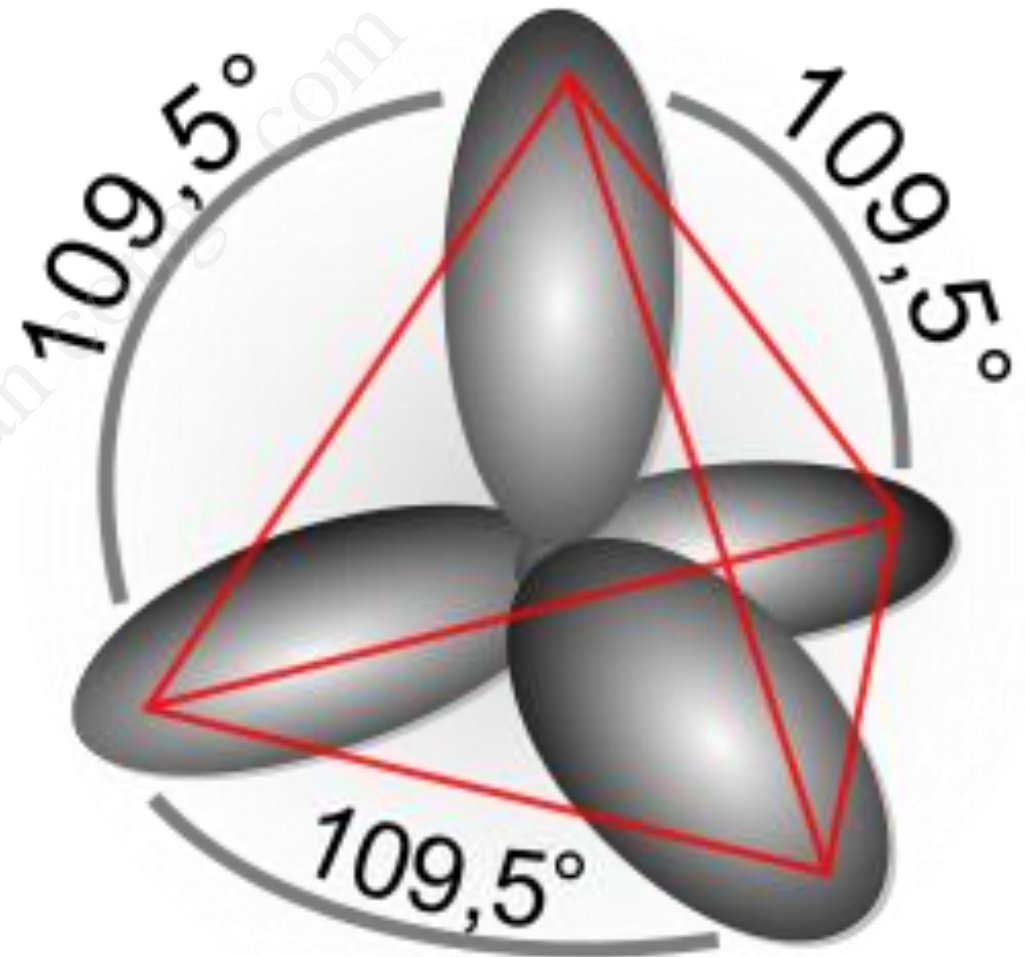


C-based solid



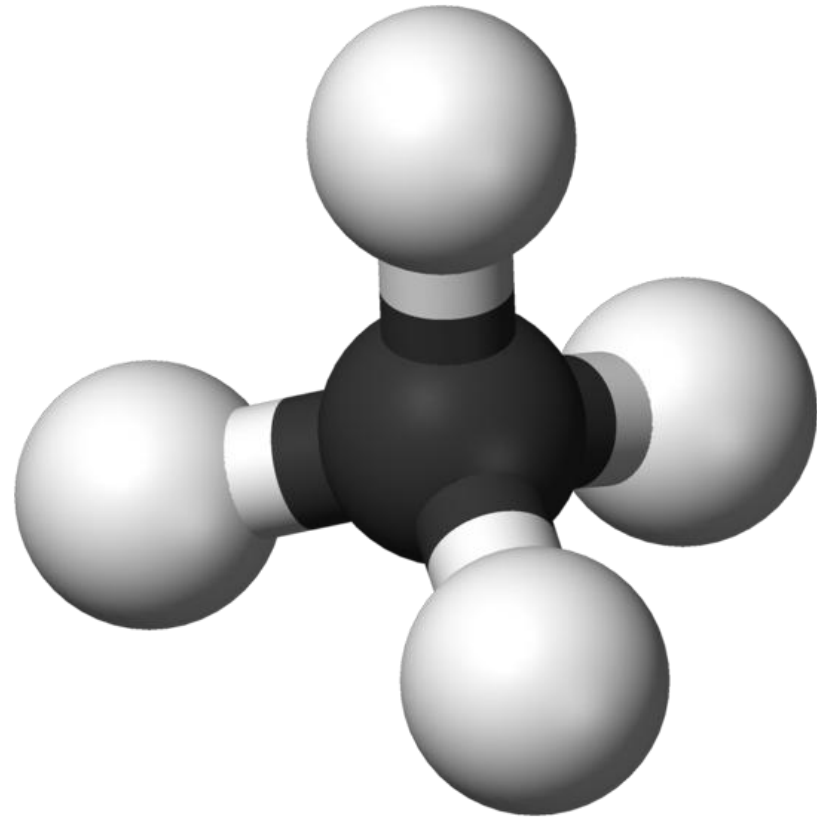
The covalent bond: a closer look at C

- electron configuration: 2 s and 2 p electrons
- formation of four sp^3 hybrid orbitals as linear combination between the s and three p orbitals
- directional character of p orbitals₃ is also found in sp^3 orbitals.

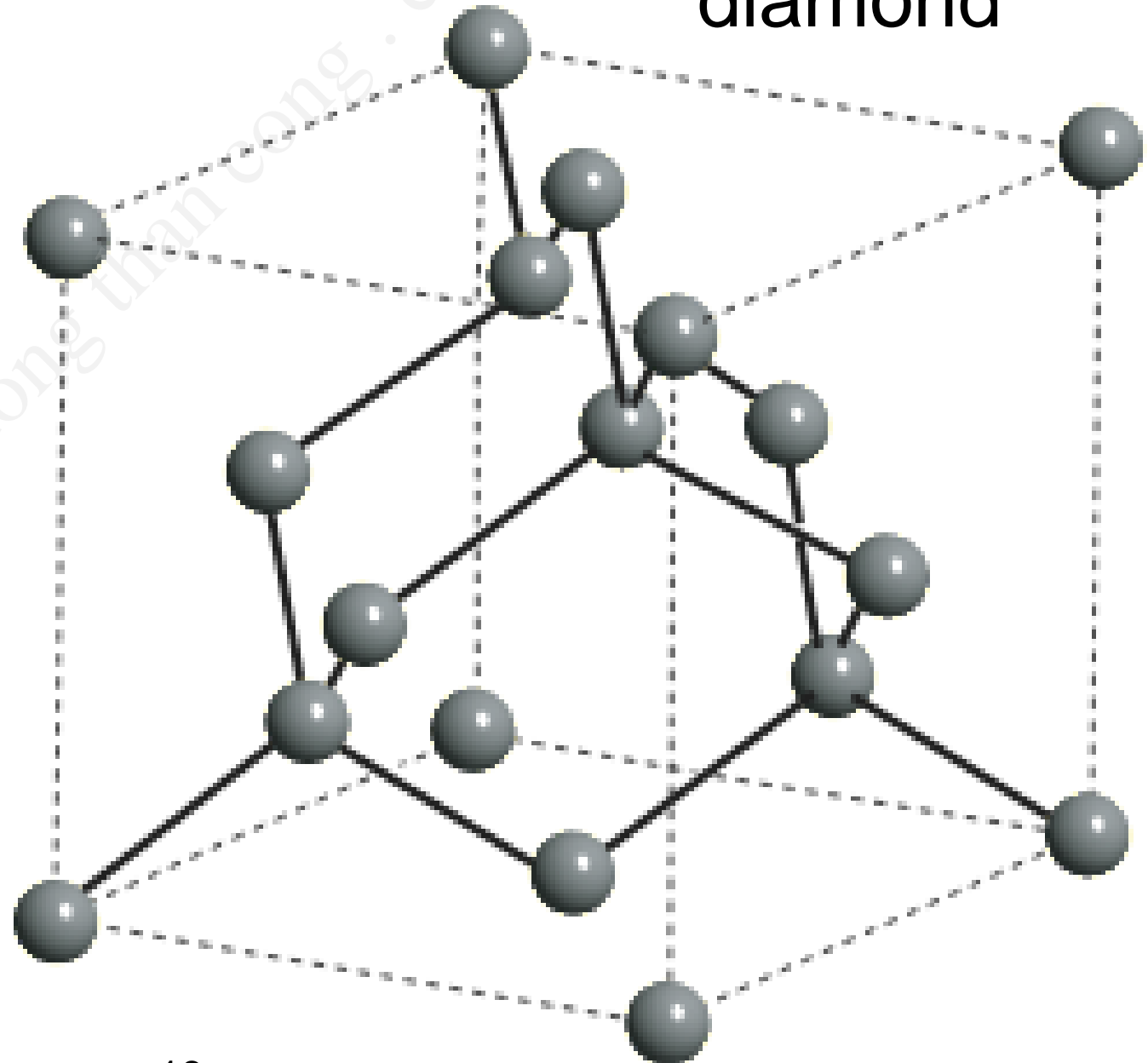


The covalent bond: sp³ bonding

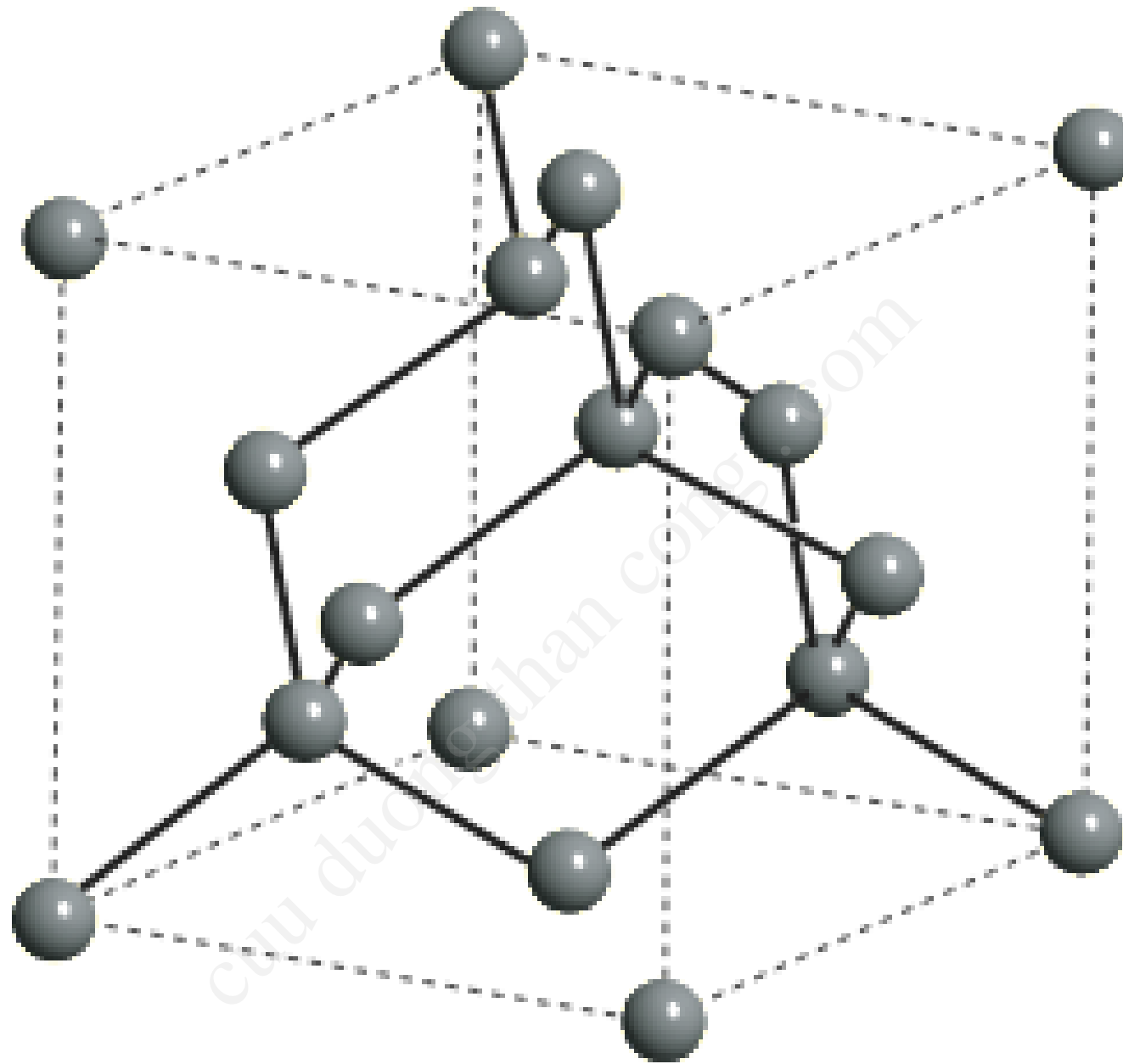
methane



diamond

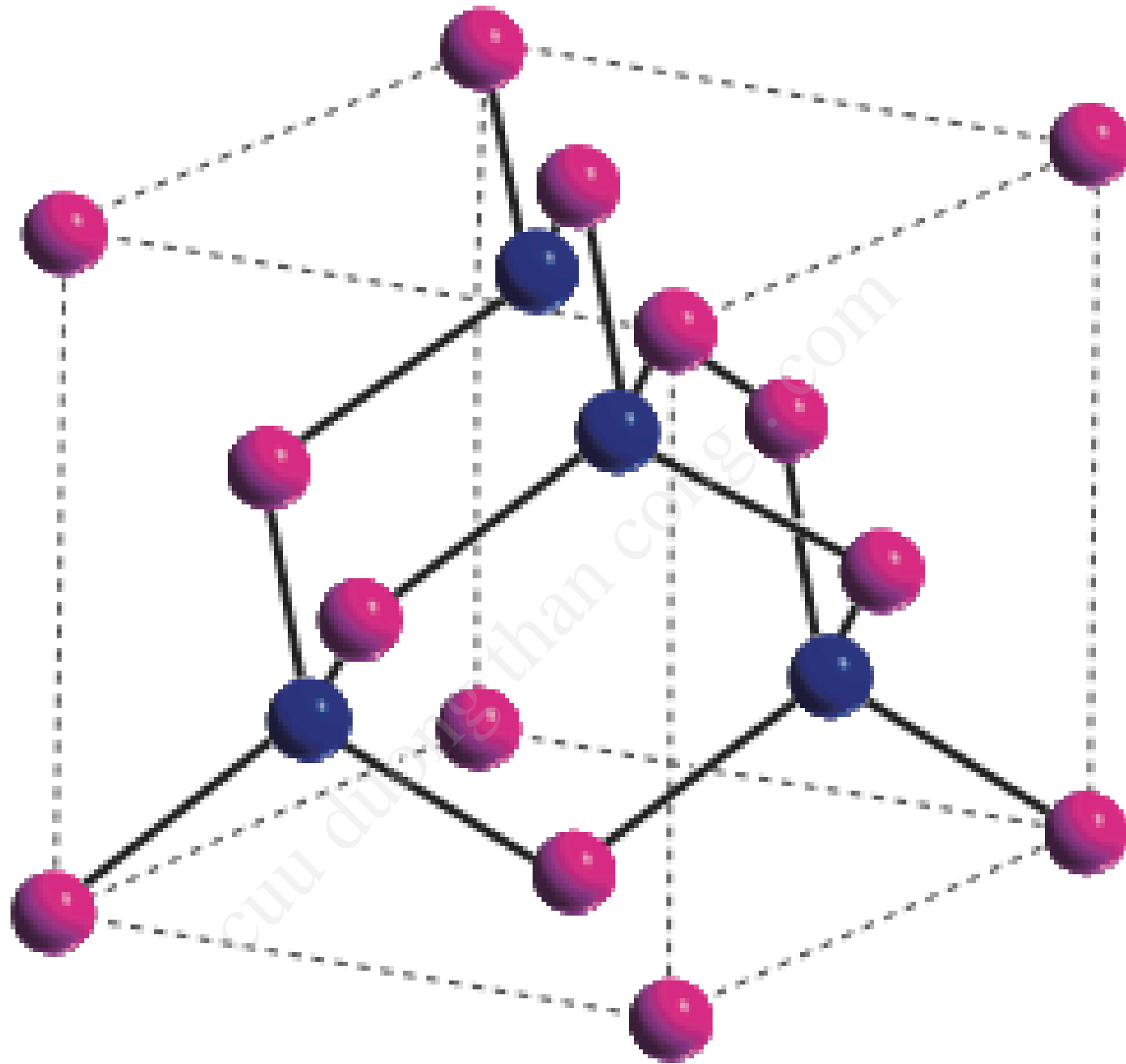


Bonding in most semiconductors



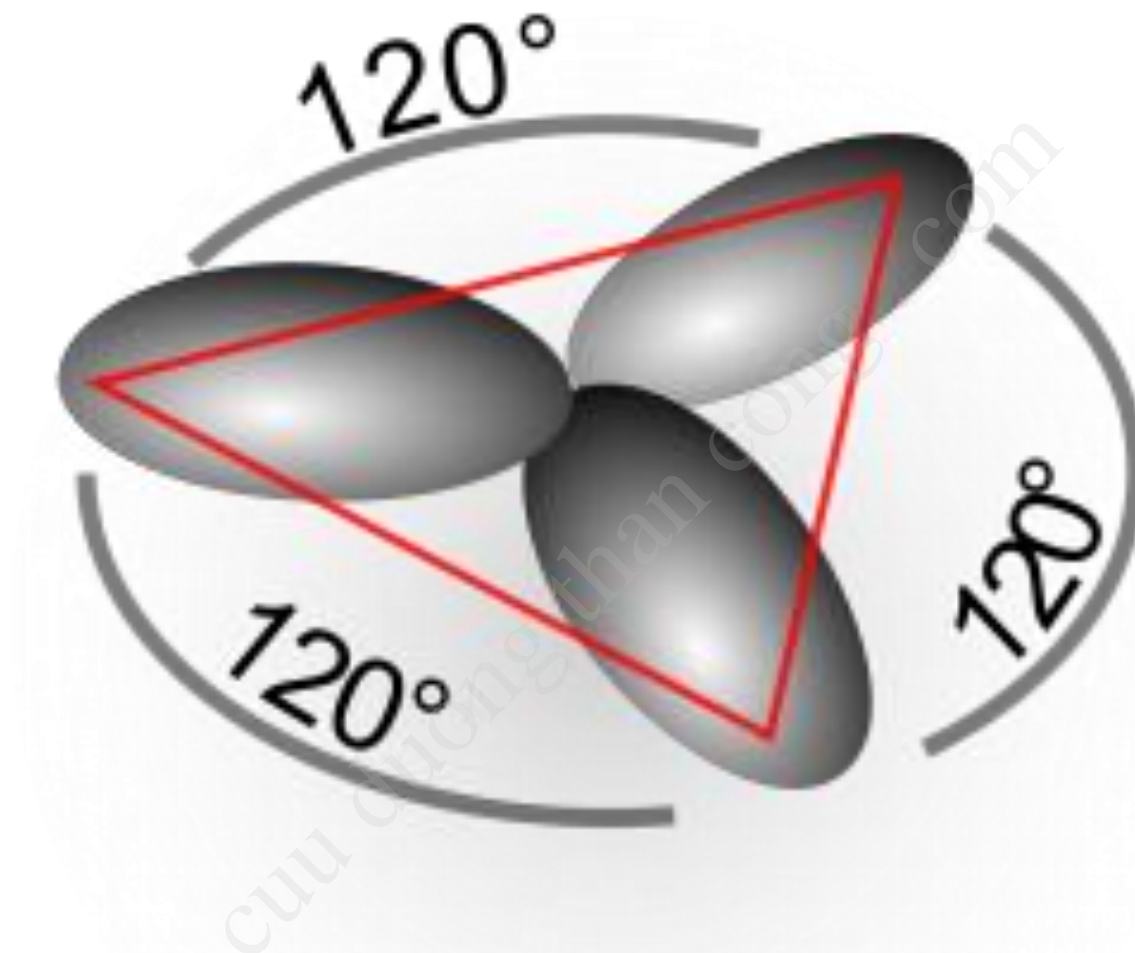
- Tetrahedral (sp^3) configuration almost ubiquitous: diamond, Si, Ge, III-V (GaAs, AlAs, InP), II-VI (CdS, CdTe)

Bonding in most semiconductors



- Tetrahedral (sp^3) configuration almost ubiquitous: diamond, Si, Ge, III-V (GaAs, AlAs, InP), II-VI (CdS, CdTe)

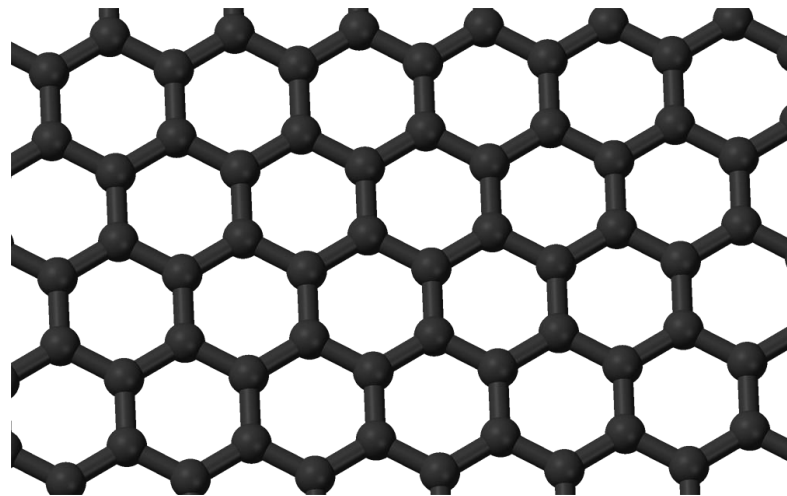
The covalent bond: sp bonding



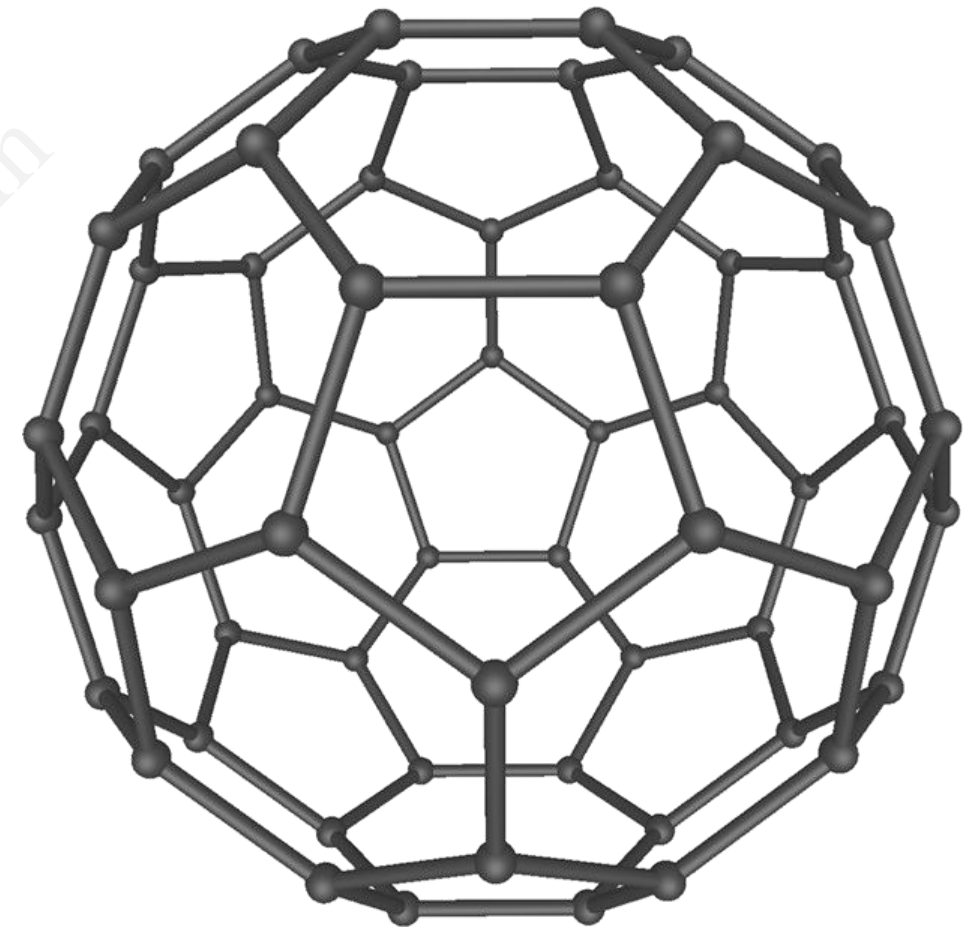
- formation of three sp² hybrid orbitals as linear combination between the s and two p orbitals. One p-orbital remains

The covalent bond: sp^2 bonding

graphene / graphite



bucky-balls



carbon nanotubes
(rolled-up graphene)



Covalent bonding

- Cohesive energies similar to ionic bonding, in the eV range.
- Very directional bonding.

Metallic bonding

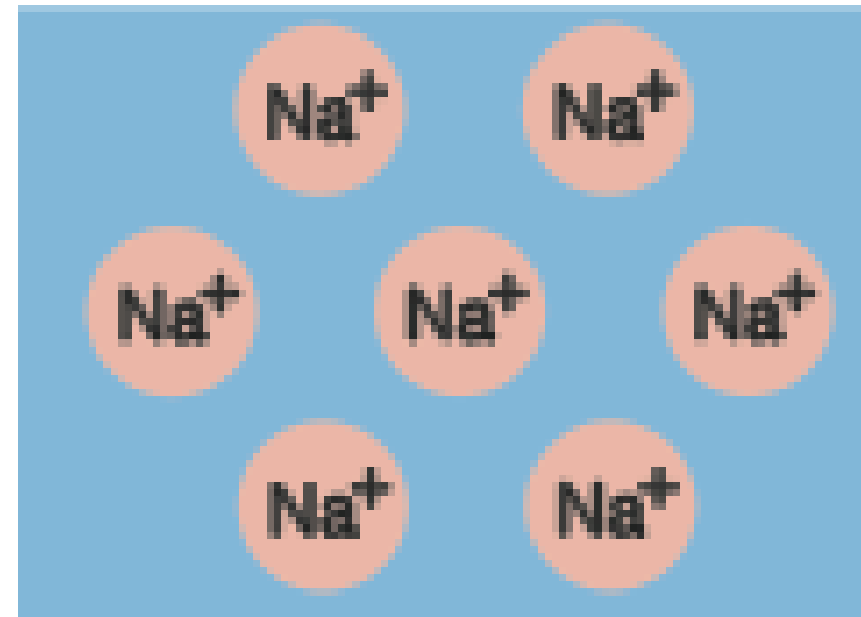
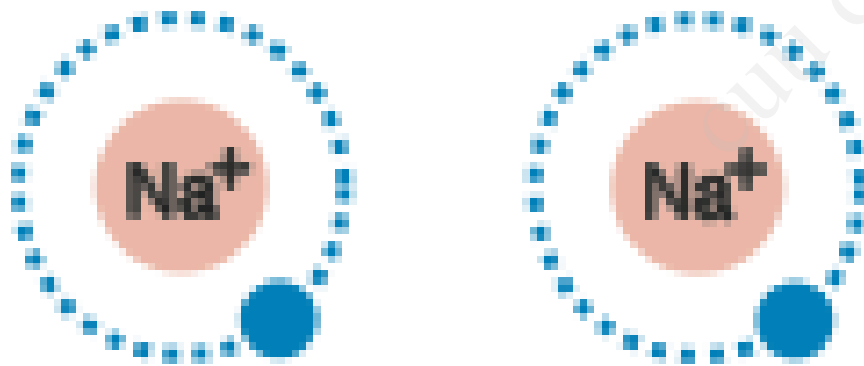
metals / non-metals

| | | | | | | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|-----|----|----|----|----|----|----|--|
| H | | | | | | | | | | | | | | | | | He | |
| Li | Be | | | | | | | | | | | B | C | N | O | F | Ne | |
| Na | Mg | | | | | | | | | | | Al | Si | P | S | Cl | Ar | |
| K | Ca | Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr | |
| Rb | Sr | Y | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I | Xe | |
| Cs | Ba | La | Hf | Ta | W | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn | |
| Fr | Ra | Ac | Rf | Db | Sg | Bh | Hs | Mt | Ds | Rg | Uub | | | | | | | |
| | | | | | | | | | | | | | | | | | | |
| | | | Ce | Pr | Nd | Pm | Sm | Eu | Gd | Tb | Dy | Ho | Er | Tm | Yb | Lu | | |
| | | | Th | Pa | U | Np | Pu | Am | Cm | Bk | Cf | Es | Fm | Md | No | Lr | | |

- the boundaries can be disputed
- simple metals, transition metals, noble metals

Metallic bonding (simple metals)

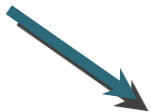
- outer electrons are delocalized and act as “glue” between positively charged ion cores
- generally found for elements with one, two or three valence electrons.
- cohesive energies in the eV range




Metallic bonding (simple metals): more characteristics

- smaller cohesive energies than in ionic crystals
- larger ionic radii, e.g. for Na: 3.82 Å (metal) and 1.94 Å (NaCl)
- bonding has no directional preference
- closed-packed atomic configurations are preferred: best possible overlap between the orbitals, no “holes” in the potential

Metallic bonding: why is this so favorable?

$$-\frac{\hbar^2 \nabla^2}{2m} \Psi(r) + U(r) \Psi(r) = E \Psi(r)$$


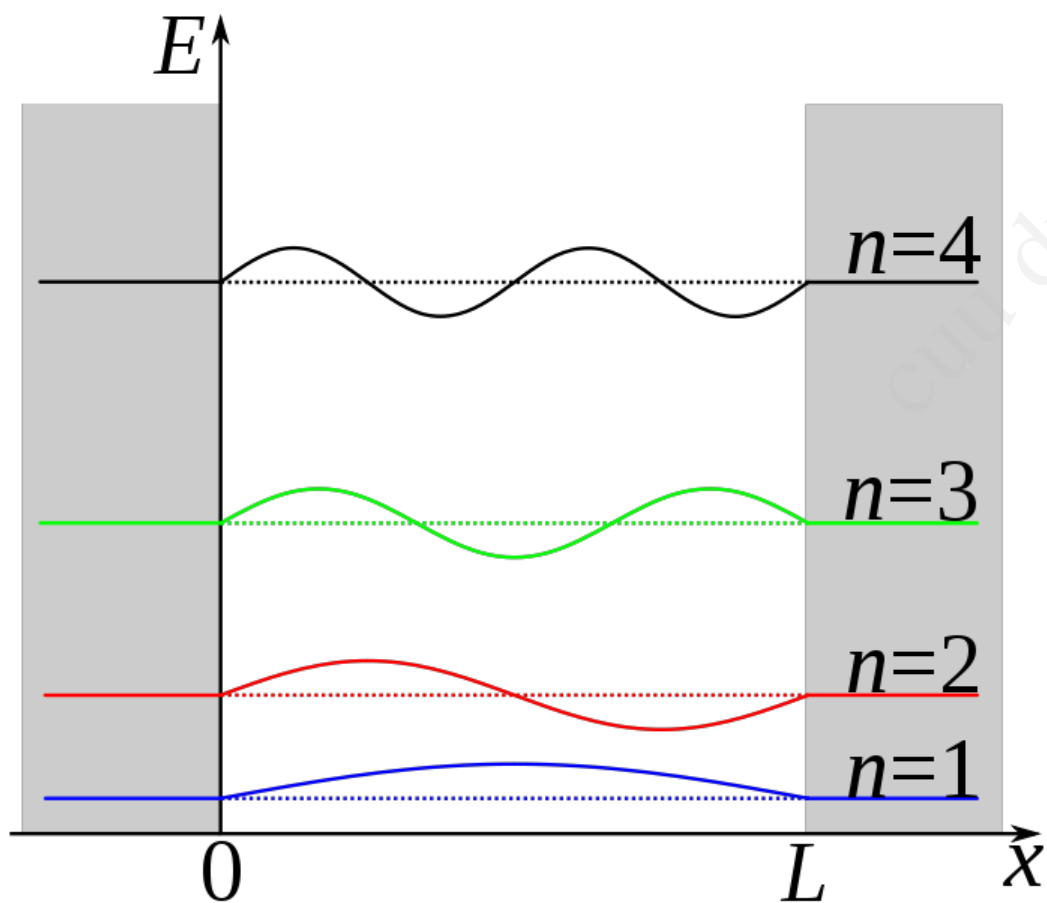
kinetic energy (or Hamiltonian for a free particle)
 \propto (negative) average curvature of wave function
“flatter” wave function \rightarrow lower energy

$$\Delta x \Delta p \geq \hbar/2$$


less localization \rightarrow smaller p variation

Metallic bonding: why is this so favorable?

$$-\frac{\hbar^2 \nabla^2}{2m} \Psi(r) + U(r) \Psi(r) = E \Psi(r)$$



Transition metals

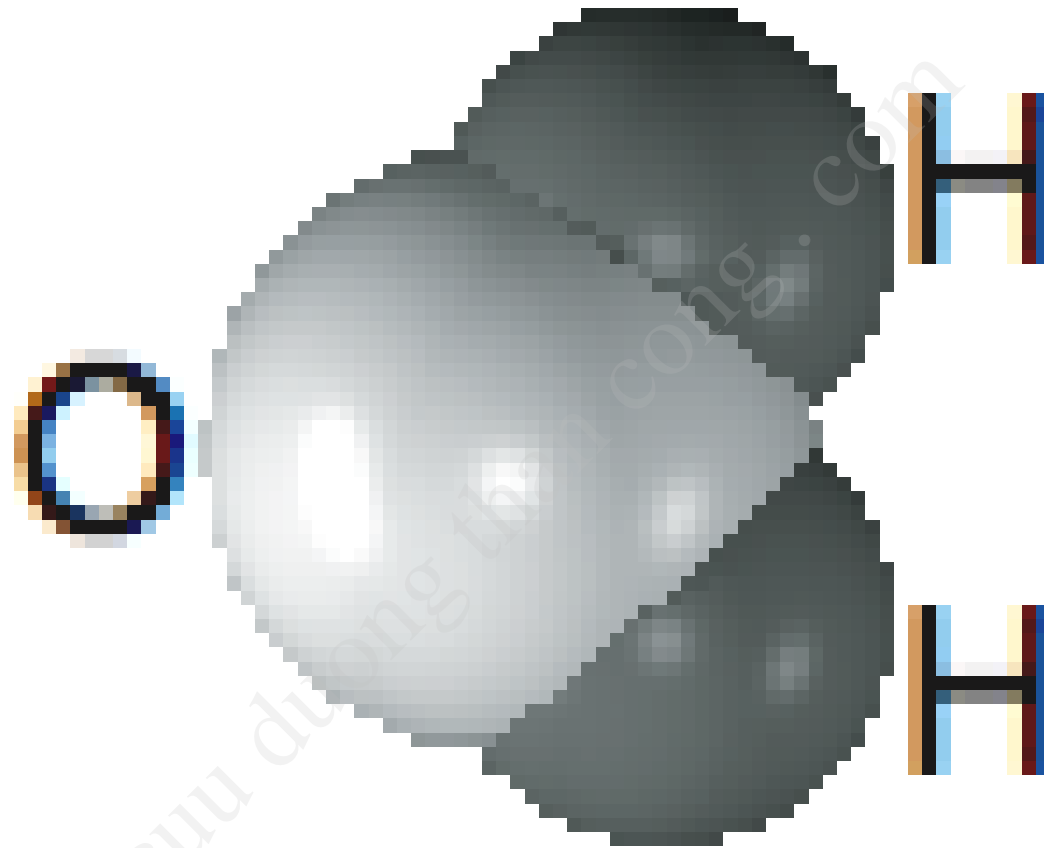
- 4s and 3d have very similar energies
- 4s electrons form delocalized metallic bonds
- 3d electrons form more local (covalent-like) bonds
- higher cohesive energies

| | | | | | | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|-----|----|----|----|----|----|----|--|
| H | | | | | | | | | | | | | | | | | He | |
| Li | Be | | | | | | | | | | | B | C | N | O | F | Ne | |
| Na | Mg | | | | | | | | | | | Al | Si | P | S | Cl | Ar | |
| K | Ca | Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr | |
| Rb | Sr | Y | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I | Xe | |
| Cs | Ba | La | Hf | Ta | W | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn | |
| Fr | Ra | Ac | Rf | Db | Sg | Bh | Hs | Mt | Ds | Rg | Uub | | | | | | | |
| | | | | | | | | | | | | | | | | | | |
| | | | Ce | Pr | Nd | Pm | Sm | Eu | Gd | Tb | Dy | Ho | Er | Tm | Yb | Lu | | |
| | | | Th | Pa | U | Np | Pu | Am | Cm | Bk | Cf | Es | Fm | Md | No | Lr | | |

Bonds between molecules

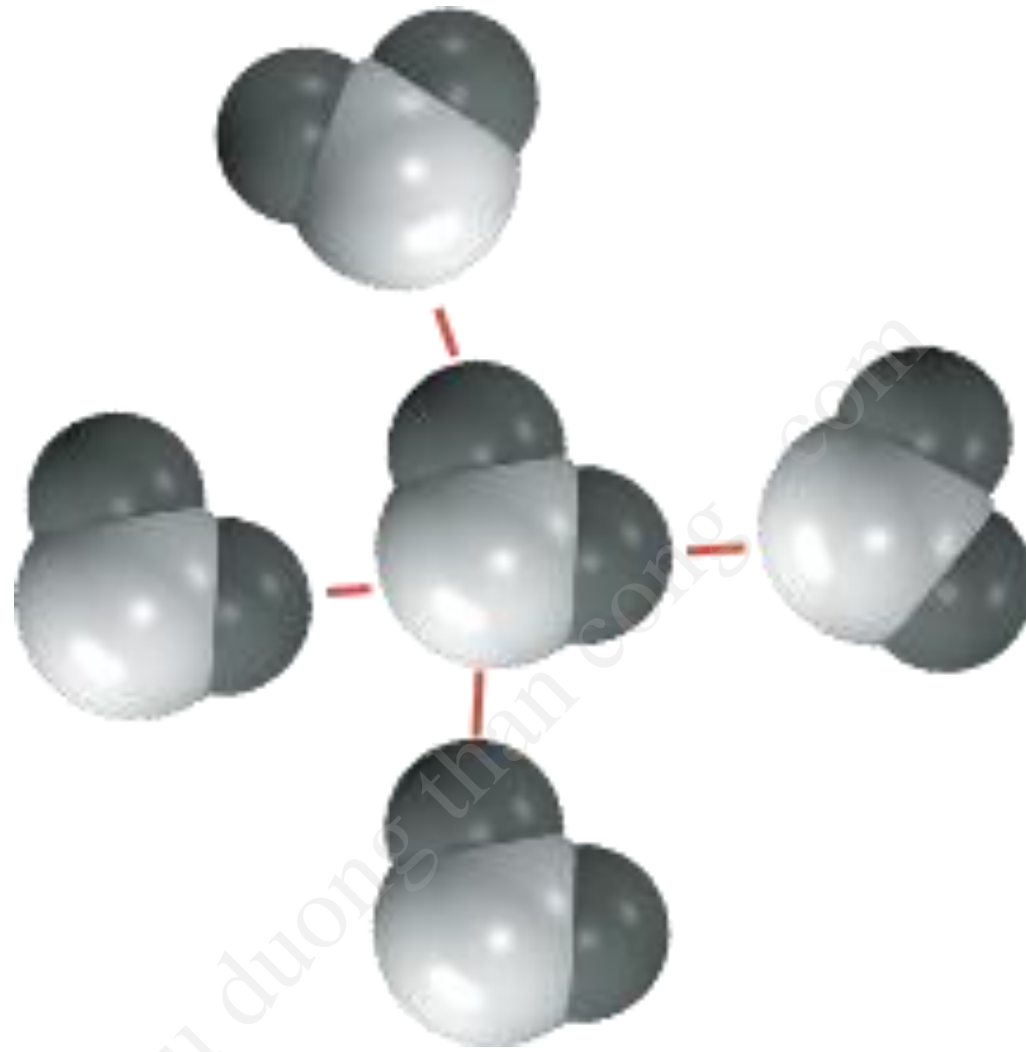
- molecular solids are very common (but not at RT)
- ice
- plastic
- DNA
- what makes molecules bond to each other?

Bonds between molecules: hydrogen bonds



permanent dipole

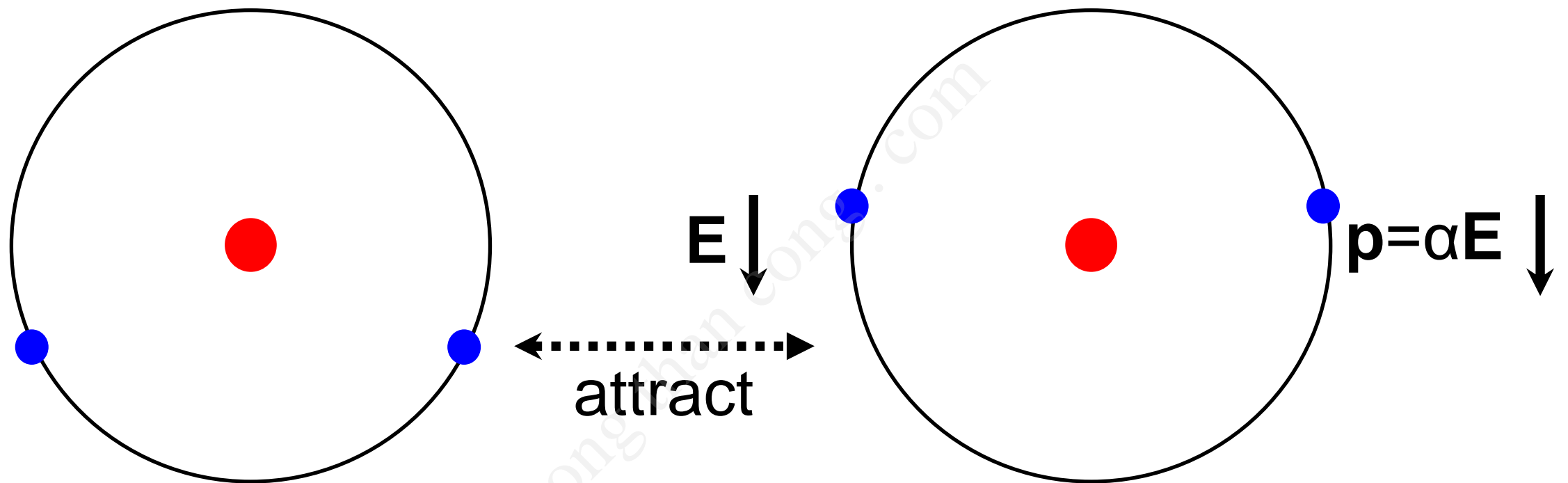
Bonds between molecules: hydrogen bonds



- H is positively charged but also very small: another “real” bond cannot be established without overlap of electron clouds (in this sense it is too big in this drawing).
- H bonding is important in ice, DNA... but not very strong

Bonds between molecules: van der Waals force

$$U = -\mathbf{E} \cdot \mathbf{p} = -\mathbf{E} \cdot \alpha \mathbf{E} \propto -\frac{1}{r^3} \alpha \frac{1}{r^3}$$

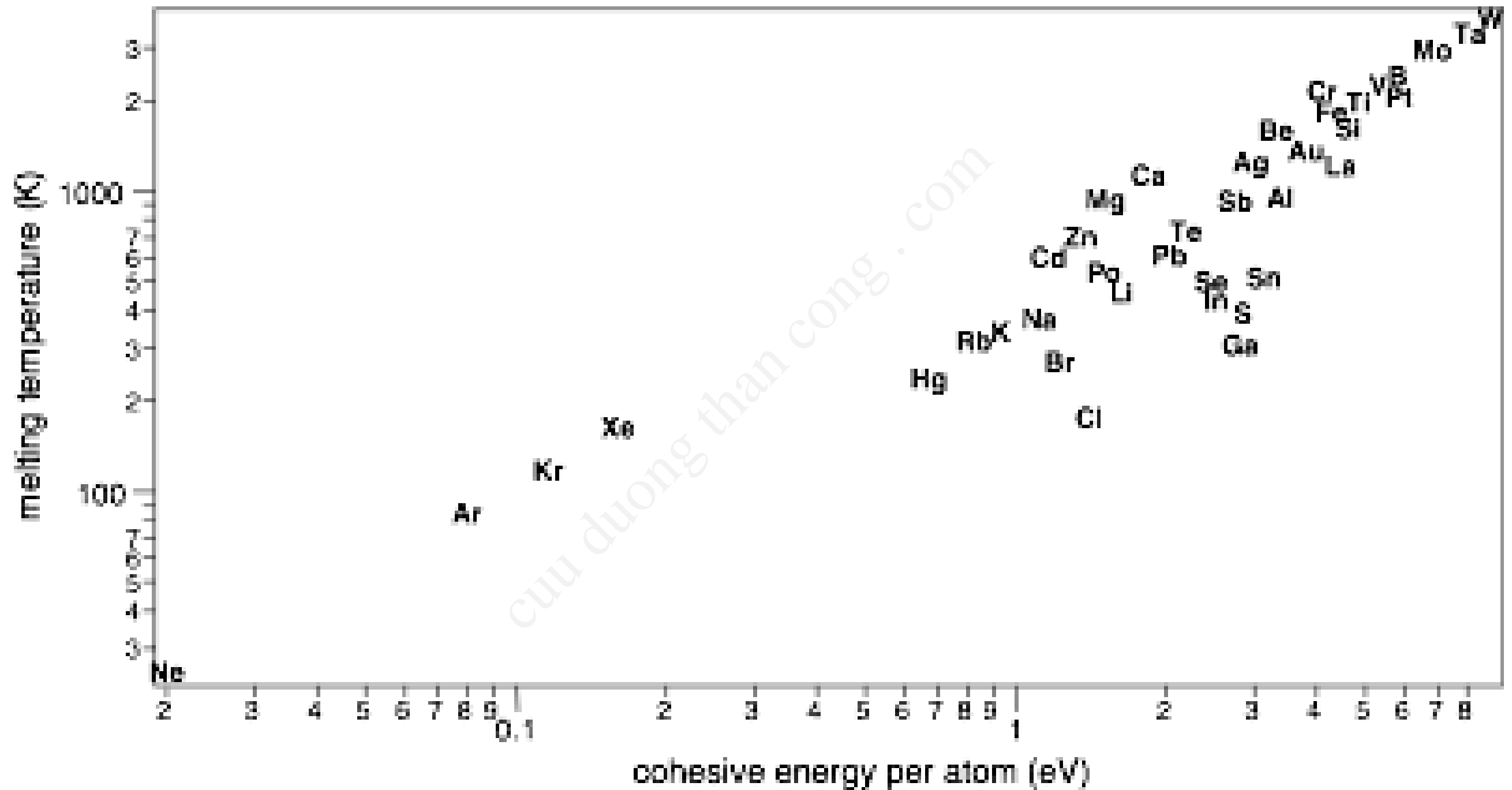


- dipole moment caused by fluctuations
- this is always present as an attractive force (even between He atoms as in this case)
- it is very weak and depends on the distance as r^{-6}

Bond type and physical properties

- How does the bond type affect the properties of a solid such as:
- mechanical strength / melting point
- electrical conductivity
- thermal conductivity
- optical properties

Bond type and physical properties



Summary

- We have looked at different types of bonding: ionic, metallic, covalent, H-bonds, van der Waals bonds.
- In reality, intermediate bonding scenarios are often found.
- We have some ideas about the relation between the bonding type and the physical properties (at least for the melting point).